Quantized Fusion Rules for Energy-Based Distributed Detection in Wireless Sensor Networks

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> IEEE SSPD' 2014 Session 5: Distributed Signal Processing

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Introduction



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- Soft Decision Fusion Rules

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Motivation

• Distributed detection has been attracting significant interest in the context of WSNs [Chamberland 2007] and [Barbarossa 2013].

Challenges

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Distributed Detection in WSN

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- To improve the detection by fusing the measurements provided by various SNs in a manner that:
 - Efficiently utilizes the scarce bandwidth.
 - Overcomes the limitations of a fading wireless channel.

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Literature Review

• Chamberland addressed the decentralized detection in bandwidth constrained sensor networks, where the design of sensor messages sent to the FC that minimize the error probability is investigated [Chamberland 2003].

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- Xiao and Luo investigated the problem of detecting a known deterministic parameter under restricted channel capacity [Xiao 2005].
- The channel fading effect on distributed detection was tackled by Chenn [Chenn 2006].
- Barbarossa and Sardelliti addressed both issues of limited bandwidth and channel imperfections. They optimized the transmission power for the detection of a known signal [Barbarossa 2013].

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- *M* sensor nodes reporting to a FC tasked with the detection of any intruders.
- The intruder leaves a signature signal unknown to the WSN but deterministic.
- The i^{th} SN collects N samples corrupted by (AWGN) zero mean and known variance σ_i^2 .

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System Model

• Depending on the underlying hypothesis:

$$\mathcal{H}_0 : x_i(n) = w_i(n)$$

 $\mathcal{H}_1 : x_i(n) = s_i(n) + w_i(n)$

Optmimum detection

• The intruder's signal is unknown at the SNs, hence the *i*th SN estimates the energy of the received signal:

$$T_i = \sum_{n=1}^N |x_i(n)|^2.$$

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(1)

Optmimum detection

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• SNs should send their measurements to the FC, where the ultimate detection decision will be made.

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- SNs should send their measurements to the FC, where the ultimate detection decision will be made.
- Available bandwidth is limited.
- This approach is not always feasible in the context of WSNs .



Optmimum detection

• WSN adopts a distributed detection algorithm.

Distributed Detection in WSN



Optmimum detection

- WSN adopts a distributed detection algorithm.
- SNs send their quantized soft decisions (i.e., the quantized local test statistics) to the FC.



Optmimum detection

- WSN adopts a distributed detection algorithm.
- SNs send their quantized soft decisions (i.e., the quantized local test statistics) to the FC.
- FC combines them to arrive at the global decision.

Proposition

• We propose to quantize *T_i* with *L_i* bits and transmit to the FC with power *p_i* over a wireless channel.

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Proposition

- We propose to quantize T_i with L_i bits and transmit to the FC with power p_i over a wireless channel.
- The number of quantization bits at the *i*th SN must satisfy the channel capacity constraint:

$$L_i \leq \frac{1}{2}\log_2\left(1+\frac{p_ih_i^2}{\zeta_i}\right)$$
 bits, $i=1,2,\ldots,M$.

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• The wireless channel conditions between the *i*th SN and the FC:

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The wireless channel conditions between the *ith* SN and the FC:
 Suffers from zero mean AWGN with a variance of ζ_i.

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The wireless channel conditions between the *ith* SN and the FC:
 Suffers from zero mean AWGN with a variance of ζ_i.
 Experiences flat fading with a channel gain h_i (assumed to be iid).

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Part I Soft Decision Fusion Rules

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Optimal Fusion Rule cont'd ...

• Optimal soft decision fusion rule is investigated given infinite bandwidth for each WSN (no quantization is required).

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Optimal Fusion Rule cont'd ...

- Optimal soft decision fusion rule is investigated given infinite bandwidth for each WSN (no quantization is required).
- Given the local soft test statistic:

$$T_i = \sum_{n=1}^N |x_i(n)|^2.$$

(2)

Optimal Fusion Rule cont'd ...

- Optimal soft decision fusion rule is investigated given infinite bandwidth for each WSN (no quantization is required).
- Given the local soft test statistic:

$$T_i = \sum_{n=1}^{N} |x_i(n)|^2.$$

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• The optimal fusion rule follows from the likelihood ratio test:

LRT
$$(\mathbf{T}) = \frac{p\{T_1, T_2, ..., T_M | \mathcal{H}_1\}}{p\{T_1, T_2, ..., T_M | \mathcal{H}_0\}} \ge \gamma$$
 (3)

where $p\{T_1, T_2, ..., T_M | \mathcal{H}_j\}$ is the joint probability distribution of local soft decisions under the j^{th} hypothesis.

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Optimal Fusion Rule cont'd ...

• *T_i* can be adequately approximated by a Gaussian distribution with the following mean and variance:

$$\mathbb{E} \{ T_i | \mathcal{H}_0 \} = N \sigma_i^2, \\ \mathbb{E} \{ T_i | \mathcal{H}_1 \} = N \sigma_i^2 (1 + \xi_i),$$

 $\operatorname{Var} \{ T_i | \mathcal{H}_0 \} = 2N\sigma_i^4$ (4) $\operatorname{Var} \{ T_i | \mathcal{H}_1 \} = 2N\sigma_i^4 (1+2\xi_i)$

where $\xi_i = \sum_{n=1}^{N} s_i^2(n) / N \sigma_i^2$ is the SNR at the *i*th SN.

(5)

Optimal Fusion Rule cont'd ...

• *T_i* can be adequately approximated by a Gaussian distribution with the following mean and variance:

$$E \{ T_i | \mathcal{H}_0 \} = N \sigma_i^2, \qquad \operatorname{Var} \{ T_i | \mathcal{H}_0 \} = 2N \sigma_i^4$$

$$E \{ T_i | \mathcal{H}_1 \} = N \sigma_i^2 (1 + \xi_i), \qquad \operatorname{Var} \{ T_i | \mathcal{H}_1 \} = 2N \sigma_i^4 (1 + 2\xi_i)$$

$$(4)$$

where
$$\xi_i = \sum_{n=1}^{N} s_i^2(n) / N \sigma_i^2$$
 is the SNR at the *i*th SN.

• Noise at different SNs assumed independent, LLR takes the form:

$$T_f = \sum_{i=1}^{M} \left(\frac{\left(T_i - N\sigma_i^2\right)^2}{2N\sigma_i^4} - \frac{\left(T_i - N\sigma_i^2\left(1 + \xi_i\right)\right)^2}{2N\sigma_i^4\left(1 + 2\xi_i\right)} \right) \ge \gamma' \quad (6)$$

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(5)

Optimal Fusion Rule

• The LLR can be further simplified

$$T_f = \sum_{i=1}^M a_i \left(T_i - b_i \right)^2$$

(7)

$$a_i = rac{\xi_i}{N\sigma_i^4 \left(1 + 2\xi_i\right)}, \quad b_i = rac{N\sigma_i^2}{2}.$$

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 $M\sigma^2$

(7)

$$\mathbf{a}_{i} = \frac{\zeta_{i}}{N\sigma_{i}^{4}\left(1 + 2\xi_{i}\right)}, \quad \mathbf{b}_{i} = \frac{N\sigma_{i}}{2}.$$
• where $\gamma' = 2\ln\left(\prod_{i=1}^{M}\gamma\left(\frac{\sqrt{2N\sigma_{i}^{4}}}{\sqrt{2N\sigma_{i}^{4}(1+2\xi_{i})}}\right)\right)$.

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Suboptimal Fusion Rules cont'd ...

Suboptimal Fusion Rules

• The optimal fusion rule requires the exact knowledge of the SNR (ξ_i) .

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- We propose three suboptimal rules:
 - Weighted fusion
 - 2 Equal fusion
 - Optimum linear fusion

Weighted Fusion Rule

• Replace a_i by $a_i^w = 1/2N\sigma_i^4$ and we let $b_i^w = b_i = \frac{N\sigma_i^2}{2}$. This rule approaches the optimal one when the SNR is large.

$$T_f = \sum_{i=1}^{M} a_i (T_i - b_i)^2$$
 (8)

Equal Weight Fusion Rule

Optimum Linear Fusion Rule

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Equal Weight Fusion Rule

•
$$a_i^e = 1$$
 for all $i = 1, 2, \cdots, M$. Also, $b_i^e = b_i$.

Optimum Linear Fusion Rule

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Optimum Linear Fusion Rule

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$$T_f^l = \sum_{i=1}^M \alpha_i T_i$$
, where $\alpha_i = \frac{\xi_i}{N\sigma_i^2(1+2\xi_i)}$.
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Part II Quantized Soft Decision Fusion Rules

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Quantized Optimal Fusion Rule cont'd ...

• Previously we assumed infinite bandwidth is available to send the exact *T_i* to FC.

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Quantized Optimal Fusion Rule cont'd ...

- Previously we assumed infinite bandwidth is available to send the exact *T_i* to FC.
- Now let the quantized test statistic (*T̂_i*) at the *ith* sensor be modeled (with *L_i* bits) as

$$\hat{T}_i = T_i + v_i \tag{9}$$

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$$\hat{T}_i = T_i + v_i \tag{9}$$

• v_i is the quantization noise with uniform distribution in the interval [-B, B] and variance B^2

$$\sigma_{\nu_i}^2 = \frac{B^2}{3 \times 2^{2L_i}}.$$
 (10)

Quantized Optimal Fusion Rule

• Approximating \hat{T}_i 's as Gaussian distribution, the LLR optimum fusion rule can be shown to be:

$$T_{f}^{q} = \sum_{i=1}^{M} a_{i}^{q} \left(\hat{T}_{i} - b_{i}^{q}\right)^{2}$$
 (11)

$$a_i^q = \frac{\xi_i}{N\sigma_i^4 \left(1 + 2\xi_i + \frac{\sigma_{\widetilde{V}_i}^2}{2N\sigma_i^4}\right) \left(1 + \frac{\sigma_{\widetilde{V}_i}^2}{2N\sigma_i^4}\right)}$$

 $b_i^q = \frac{N\sigma_i^2}{2} - \frac{\sigma_{v_i}^2}{4\sigma^2}.$

Observations

• Note that
$$T_f^q \to T_f$$
 as $\sigma_{v_i}^2 \to 0$ for all *i*.

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- Interesting observation is that $T_f^q \to T_f$ as $N \to \infty$, regardless of $\sigma_{v_i}^2$.

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- Consequently, $a_i^q \rightarrow a_i$ and $b_i^q \rightarrow b_i$ under the previous condition.
- Interesting observation is that $T_f^q \to T_f$ as $N \to \infty$, regardless of $\sigma_{v_i}^2$.
- Bandwidth can be saved but at the expense of increasing both the number of collected measurements and also the detection delay.

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Quantized Sub-Optimum Fusion Rules

$$T_f^q = \sum_{i=1}^M a_i^q \left(\hat{T}_i - b_i^q\right)^2$$

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Quantized Sub-Optimum Fusion Rules

$$T_f^q = \sum_{i=1}^M a_i^q \left(\hat{T}_i - b_i^q\right)^2$$

• The suboptimal (quantized) fusion rules can be easily shown to be:

$$L_i \leq \frac{1}{2} \log_2 \left(1 + \frac{\rho_i h_i^2}{\zeta_i}\right)$$
 bits, $i = 1, 2, \dots, M$.

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• Weighted fusion
$$:a_i^q = a_i^{wq} = \frac{1}{N\sigma_i^4 \left(1 + \frac{\sigma_{v_i}^2}{2N\sigma_i^4}\right)^2}.$$

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$$:a_i^q = a_i^{wq} = \frac{1}{N\sigma_i^4 \left(1 + \frac{\sigma_{V_i}^2}{2N\sigma_i^4}\right)^2}.$$

• Equal fusion: $a_i^q = a^{eq} = 1$ and $b^{eq} = b^{wq}_{wq} = b_i^q$.

$$L_i \leq \frac{1}{2} \log_2 \left(1 + \frac{p_i h_i^2}{\zeta_i} \right)$$
 bits, $i = 1, 2, \dots, M$.

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Quantized Soft Decision Fusion Rules

Quantized Linear Fusion Rule

$$T_f^l = \sum_{i=1}^M \alpha_i^q \, \hat{T}_i$$

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Quantized Soft Decision Fusion Rules

Quantized Linear Fusion Rule

$$T_f^I = \sum_{i=1}^M \alpha_i^q \, \hat{T}_i$$

 The weights of suboptimal (quantized) linear fusion rules can be easily shown to be:

$$\alpha_i^q = \frac{\xi_i}{2\sigma_i^2 \left[1 + 2\xi_i + \frac{\sigma_{\nu_i}^2}{N\sigma_i^2}\right]}.$$
(12)

E. Nurellari, D. McLernon, M. Ghogho and S. Aldalahmeh, "Optimal quantization and power allocation for energy-based distributed sensor detection," *Proc. EUSIPCO*, Lisbon, Portugal, 1-5 Sept. 2014.

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- A natural one is the probability of detection, which depends on the distribution of the fusion rule.
- Letting $U_i = \left(\hat{T}_i b_i\right)^2$ then the optimum fusion rule can be written as M

$$T_f^q = \sum_{i=1} a_i^q U_i.$$
(13)

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- A natural one is the probability of detection, which depends on the distribution of the fusion rule.
- Letting $U_i = (\hat{T}_i b_i)^2$ then the optimum fusion rule can be written as

$$T_{f}^{q} = \sum_{i=1}^{m} a_{i}^{q} U_{i}.$$
 (13)

• Using the central limit theorem, T_f^q can be approximated by a Gaussian distribution:

$$\mathcal{T}_{f}^{q} \sim \begin{cases} \mathcal{N}\left(\mathrm{E}\left\{\mathcal{T}_{f}^{q}|\mathcal{H}_{0}\right\}, \mathrm{Var}\left\{\mathcal{T}_{f}^{q}|\mathcal{H}_{0}\right\}\right) \mathrm{under} \ \mathcal{H}_{0} \\ \mathcal{N}\left(\mathrm{E}\left\{\mathcal{T}_{f}^{q}|\mathcal{H}_{1}\right\}, \mathrm{Var}\left\{\mathcal{T}_{f}^{q}|\mathcal{H}_{1}\right\}\right) \mathrm{under} \ \mathcal{H}_{1} \end{cases}$$
(14)

Optimum Sensor Transmit Power Allocation

Optimization Problem

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$$\boldsymbol{p}_{opt} = \arg \max_{\boldsymbol{p}} P_d(\boldsymbol{p})$$

subject to $\sum_{i=1}^{M} p_i \le P_t$ for $p_i \ge 0, i = 1, \dots, M$ (1)

where $p = [p_1, p_2, ..., p_M]$.

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• We adopt the spatial branch-and-bound strategy using the YALMIP optimization tools.

Overview

1 Introduction

- 2 Problem Formulation
- 3 Soft Decision Fusion Rules
- 4 Quantized Soft Decision Fusion Rules
- 5 Optimum Sensor Transmit Power Allocation

6 Simulation Results

7 Conclusions

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Simulations setup

- We simulate a WSN of *M* SNs detecting an intruder with $s_i(n) = A$, where A = 0.1.
- The communication noise variances set to $\zeta_i = 0.1 \ \forall i$ (for simplicity).
- The measurement noise variances are generated randomly and used throughout the simulations.
- The average measurement SNR for the network is defined as $\xi_a = 10 \log_{10} \left(\frac{1}{M} \sum_{i=1}^{M} \xi_i \right).$
- In all simulations we assume perfect knowledge of ξ_i .

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Simulation Results 1/6



Simulation Results 2/6



Simulation Results 3/6



Simulation Results 4/6



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Simulation Results 5/6



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Simulation Result 6/6



Figure: Optimum sensor transmit power and channel quantization bits allocation for N = 10, $P_{fa} = 0.1$, $\xi_a = 8.5$ dB and $P_t = 20$.

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- We show that the effect of quantization on the detection performance can be mitigated by increasing the number of measurements (*N*), or equivalently incurring more delay in the system.
- Finally, the SN's transmission power has been optimally allocated. Intuitively, more power is given to SNs having better channel gains and consequently increased number of bits.

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Questions/Comments?

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